## $\mathbf{M}+\mathbf{A}+\mathbf{T}+\mathbf{H}=$ love

## NIO) $\overrightarrow{1}$ 代B) L Nombers

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## FRIEDMAN NUMBERS

A Friedman number is a positive integer that can be written in some nontrivial way using its own digits together with the elementary operations ( $+,-, x, 1$, exponents, and grouping symbols).

There is only one Friedman number under 100.


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## FIND FIVE MORE

$$
\begin{aligned}
& \text { However, there are five } \\
& \text { Friedman numbers in the } \\
& \text { 120s. Can you find all five? }
\end{aligned}
$$

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$$

## SOURCES

- Number Freak : from 1 to 200 : The Hidden Language of Numbers Revealed by Derrick Niederman - 2009 - Penguin
- NCTM Illuminations - Brainteaser
- Erich Friedman - Problem of the Month - August 2000
- "Finding Friedman Numbers - Stem.org.uk


## HAPPY

 NUME=5B
## $\mathbf{M}+\mathbf{A}+\mathbf{T}+\mathbf{H}=$ love

## HAPPY NUMBERS

- Pick a number.
- Square each digit and add the result together.
- Use the new number and do the same again.
- If you reach 1 , you have a HAPPY NUMBER.
- If you never reach 1 , you have a SAD NUMBER.


## M <br> $+\mathbf{A}$ <br> $A+$ T <br> $+$ <br> H

# HAPPY NUMBERS 

## Is 13 a happy number?

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## HAPPY NUMBERS



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## HAPPY NUMBERS

- What is the smallest sad number?
- What is the smallest happy prime number?

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## BREAKOUT ROOMS

What percent of the numbers 1-100 are happy?

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

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## EXTENSION TASKS

- Is there an infinite number of happy numbers or is there a largest happy number?
- What is the smallest integer greater than 1 that, when multiplied by any happy number yields another happy number?
- Are there any pairs of consecutive numbers that are both happy? Are there strings of more than two consecutive numbers that are happy?
- What digit does not show up in any of the happy numbers under 100 ? Why is this? What is the smallest happy number containing this digit?


## EXTENSION TASKS

- Does happiness depend on the base in which the number is written?
- What is the maximum number of steps it takes to determine if a number is happy or sad?
- Investigate what happens when you apply the steps but cube the numbers instead of squaring them. What name would you give this type of number?


## SOURCES

- MathCounts Problem of the Week Archive - Happy Numbers - August 29, 2016
- Fred and Amy's Maths Shack - Happy Numbers
- "Happy Lessons" by Luke Robinson - Mathematics Teaching - September 2006 Issue 198
- "Happy Integers" by Donald C. Duncan - The Mathematics Teacher - November 1972 - Vol 65 Issue 7
- Numbers are Forever by Liz Strachan - 2014 - Constable - Pages 107-108


## M <br> $+\mathbf{A}$

